# Cationic Radius Ratio and Formation of K<sub>2</sub>NiF<sub>4</sub>-Type Compounds

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A survey of known compounds which can assume  $K_2NiF_4$ -type structure at least over a certain P, T range was made. The cationic radius ratios  $r_A/r_B$  of this family of compounds were found to vary over a relatively narrow range of values around 2.00, in contrast to the much wider ranges known for other important  $A_2BX_4$  structure groups, e.g.,  $\beta$ -K<sub>2</sub>SO<sub>4</sub>, thenardite, olivine, etc., providing thereby a constraint on the crystal chemical variabilities in this group of compounds. Usefulness of the simple size parameter  $r_A(IX)/r_B(VI)$  in predicting formation of new K<sub>2</sub>NiF<sub>4</sub>-type compounds is discussed.

## Introduction

The compound  $K_2NiF_4$  crystallizes in the tetragonal space group I4/mmm (1) in which octahedrally coordinated Ni<sup>2+</sup> ions form extended sheets along (001), interspersed with two layers of much larger  $K^+$ ions in ninefold coordination with fluorine. A large number of isotypes of this compound are known. Current interest in these layer-type compounds stems from the reported two-dimensional antiferromagnetic behavior of  $K_2NiF_4$  (2). A survey of the known K<sub>2</sub>NiF<sub>4</sub>-type compounds was undertaken in search of some characteristic parameters governing formation of this structure among  $A_2BX_4$  compounds. The results show that the size ratio of the cations,  $r_A(IX)/r_B(VI)$ , serves this purpose to a reasonably good extent.

## **Cationic Radius Ratios and Their Ranges**

The major stoichiometries with known Aand B-site occupants are shown in Table I. It must be pointed out, however, that only about 45% of the total number of possible A-B combinations in Table I lead to the formation of  $K_2NiF_4$ -type compounds. Among the rest, there are several forbidden A-B combinations which give rise to non- $K_2NiF_4$ -type structures, e.g.,  $Ba_2TiO_4$ ,  $Ba_2CrO_4$ ,  $Ba_2FeO_4$ ,  $Sr_2PbO_4$ ,  $Ca_2PbO_4$ ,  $Ca_2IrO_4$ , and  $Ca_2SnO_4$  (4, 5) in group 2, and  $Cs_2MgCl_4$  (19) in group 7; crystallographic information about some others (e.g.,  $BaLnB^{3+}O_4$ , where  $B = Al^{3+}$ ,  $Cr^{3+}$ ,  $Fe^{3+}$ , etc.) is apparently unavailable. Additional compounds not considered in Table I include some oxyfluorides, chlorobromides, and chloroiodides (5, 6, 18, 21). Oxygen and fluorine, however, remain by far the most dominant occupants of the X-site.

Effective ionic radius values of Shannon (7) were used for computing  $r_A(IX)/r_B(VI)$  values of known K<sub>2</sub>NiF<sub>4</sub>-type compounds (5, 6, 16, 21, 23-27). In the case of transition metals, high-spin and low-spin radii were used for divalent and trivalent *B*-ions, respectively, because (i) published information (8-10) suggests such a generalization for the trivalent ions except Fe<sup>3+</sup> (3), and (ii) preliminary plottings of  $r_A/r_B$  vs c/a showed relative self-consistencies, especially for the fluorides, when such spin states were

| Stoichiometry (1)  | Possible<br>A cations<br>(2)   | Possible<br>B cations<br>(3)   | Reference<br>(4) |
|--|--|--|------------------|
| 1. $A_2^+ B^{2+} F_4$                                    | K <sup>+</sup> , Rb <sup>+</sup> , Cs <sup>+</sup> ,<br>Tl <sup>+</sup> , NH <sup>+</sup> <sub>4</sub> | $Mg^{2+}, Ni^{2+}, Mn^{2+}, Co^{2+}, Fe^{2+}, Cd^{2+}, Zn^{2+}, Cu^{2+}$   | (5, 23)          |
| 2. $A_2^{2+}B^{4+}O_4$                                   | Ba <sup>2+</sup> , Sr <sup>2+</sup> ,<br>Ca <sup>2+</sup>  | Pb <sup>4+</sup> , Zr <sup>4+</sup> , Hf <sup>4+</sup> ,<br>Sn <sup>4+</sup> , Tc <sup>4+</sup> , Mo <sup>4+</sup> ,<br>Ir <sup>4+</sup> , Ru <sup>4+</sup> , Ti <sup>4+</sup> ,<br>Rh <sup>4+</sup> , Fe <sup>4+</sup> , Cr <sup>4+</sup> ,<br>Mn <sup>4+</sup> | (5, 23)          |
| 3. $A_2^{3+}B^{2+}O_4$                                   | Ln(=La-Gd)   | $Ni^{2+}, Cu^{2+}$   | (5)              |
| 4. $A^{2+}A^{3+}B^{3+}O_4$                               | Sr <sup>2+</sup> , Ba <sup>2+</sup> ,<br>Ca <sup>2+</sup> ,<br><i>Ln</i> (=La-Er)                      | Ni <sup>3+</sup> , Fe <sup>3+</sup> , Co <sup>3+</sup> ,<br>Mn <sup>3+</sup> , Al <sup>3+</sup> , Cr <sup>3+</sup>   | (5, 24-26)       |
| 5. $A^+ A^{3+} B^{4+} O_4$                               | $Na^+$ ,<br>Ln(=La-Lu)   | Ti <sup>4+</sup>   | (5)              |
| б. <i>А<sup>+</sup>В<sup>6+</sup></i> О4                 | $K^+$ , $Rb^+$ , $Cs^+$  | U <sup>6+</sup> , Np <sup>6+</sup>   | (5)              |
| 7. $A_2^+ B^{2+} Cl_4$                                   | $K^+$ , $Rb^+$ , $Cs^+$  | Cr <sup>2+</sup> , Mn <sup>2+</sup> , Cd <sup>2+</sup> ,<br>Mg <sup>2+</sup> , Ca <sup>2+</sup>  | (5, 18, 19)      |
| 8. $A_{1.5}^{2+}A_{0.5}^{3+}B_{0.5}^{4+}B_{0.5}^{3+}O_4$ | Ca <sup>2+</sup> ,<br>Ln(=Pr-Gd)   | $Cr^{3+}+Cr^{4+}$  | (16)             |

TABLE I MAJOR  $A_2BX_4$  Stoichiometries for  $K_2NiF_4$ -Type Structures with Possible Occupants of A and B Sites<sup>4</sup>

<sup>a</sup> Any given A cation/cation pair of column 2 may not necessarily combine with *every* B cation of column 3 to give a  $K_2NiF_4$ -type compound; see text.

assumed. However, the basic observations made here were not dependent on this choice. The cationic radius ratio was found to assume values around 2.00, varying mostly within the narrow range of 1.70 to 2.40. A comparison of this spread (~0.7) of  $r_A/r_B$ with those for other  $A_2BX_4$  structural families (5, 11, 12, 20), e.g.,  $r_A(VI)/r_B(IV)$  for olivines, yielded the following approximate values:  $\beta$ -K<sub>2</sub>SO<sub>4</sub>, 9.5; thenardite, 5; olivine, 4; spinel, 2; phenakite, 1.8. The relatively narrower spread, which is also suggested by the  $A_2BX_4$  structure field maps (5, 27), makes the  $r_A(IX)/r_B(VI)$  ratio a characteristic parameter for ascertaining if a certain  $A_2BX_4$  (X = O<sup>2-</sup>, F<sup>-</sup>; also Cl<sup>-</sup>, Br<sup>-</sup>, etc.) compound can, under some suitable P, T conditions, crystallize with a  $K_2NiF_4$ -type structure.

## Discussion

Out of more than 150 compounds assuming the K<sub>2</sub>NiF<sub>4</sub> structure, only about 5% have  $r_A/r_B$  values lying outside the prescribed range of 1.7-2.4. Most of the exceptions are below the minimum value, i.e., around 1.6-1.7, which should cause a relative decrease of the two-dimensional character. Among these,  $La_2CoO_4$ , La<sub>2</sub>CuO<sub>4</sub>, and Nd<sub>2</sub>NiO<sub>4</sub> have the tetragonal structure only at elevated temperatures (13-15). This should also be valid for the series  $CaLnCrO_4$  (Ln = Pr, Nd, Sm, Eu, Gd) where  $r_A/r_B$  values are much more favorable (16). The  $r_A(IX)/r_B(VI)$  values for hypothetical K<sub>2</sub>NiF<sub>4</sub>-type polymorphs of compounds (6, 20) belonging to other structure groups (obviously only when the A and B cations have the capability of going into ninefold and sixfold anion coordination, respectively; this excludes, for example, all the phenakite-type compounds, as well as most of the olivines and spinels) largely fall outside the prescribed range. The same is true for most of the "forbidden" A-B combinations mentioned earlier, and is probably a cause of their inability to crystallize with a K<sub>2</sub>NiF<sub>4</sub>-type structure. It is, thus, reasonable to expect that polymorphism involving this structure type will be rare in occurrence. The few known examples (5, 17, 22) undergoing temperature/pressure-induced phase inversion, i.e., Sr<sub>2</sub>CrO<sub>4</sub>, Ca<sub>2</sub>GeO<sub>4</sub>, and some CaLnGaO<sub>4</sub> phases have cationic radius ratios varying in the range 1.79–2.38, which supports our contention. Other potential candidates include the olivines NaLnGeO<sub>4</sub> (Ln = Y, Eu-Lu) and Mn<sub>2</sub>GeO<sub>4</sub>, though ninefold anion coordination of Mn<sup>2+</sup> is



FIG. 1. Variation of unit-cell volume as a function of  $r_A(IX)/r_B(VI)$ , wherever applicable, among  $A_2BX_4$  compounds (see text); field 1 is for K<sub>2</sub>NiF<sub>4</sub>-type compounds, while field 2 is a part of the area represented by  $\beta$ -K<sub>2</sub>SO<sub>4</sub>-type and related structures.

apparently unknown (7). Compounds yielding values less than 1.70 are mostly distorted forms of  $K_2NiF_4$  or isotypes of  $Sr_2PbO_4$ structure; those having higher values are mostly  $\beta$ -K<sub>2</sub>SO<sub>4</sub>-type or closely related structures. The cationic radius ratio vs cell volume plot clearly demonstrates the very restricted field for K<sub>2</sub>NiF<sub>4</sub>-type structure, as compared to that of  $\beta$ -K<sub>2</sub>SO<sub>4</sub>, only a part of which is shown in Fig. 1.

A further use of the  $r_A/r_B$  value is in suggesting new compounds which could crystallize with a K<sub>2</sub>NiF<sub>4</sub>-type structure; various new stoichiometries can be expected to do so, though those for which  $r_A/r_B$  lies comfortably within 1.9–2.3 will stand better chances. Some typical examples are: Ca<sub>2</sub>BO<sub>4</sub> ( $B = Ru^{4+}$ , Rh<sup>4+</sup>, Cr<sup>4+</sup>); BaLnAlO<sub>4</sub> (Ln =Gd-Lu); SrLnAlO<sub>4</sub> (Ln = Pm-Lu);  $A_2UO_3F$  ( $A = K^+$ , Rb<sup>+</sup>, Cs<sup>+</sup>); Ln<sub>2</sub>AlO<sub>3</sub>F (Ln = La-Ho);  $Ln_2NiO_3F$  (Ln = La-Eu); and Ba<sub>2</sub>BO<sub>2</sub>F<sub>2</sub> ( $B = Mg^{2+}$ , Ni<sup>2+</sup>, Cu<sup>2+</sup>).

The reasons for the relatively strict control of  $r_A/r_B$  in the formation of K<sub>2</sub>NiF<sub>4</sub>-type compounds can be manifold. The large difference in coordination number of A and B ions excludes ions of similar size in both the sites, and their interchange, as among the spinels; the high coordination number of Arestricts the types of cations acceptable in this site. The crystallographic restrictions put by special positions of the atoms in the lattice disallow, among others, rotation or nonsymmetrical deformation of the octahedra; this could be another controlling factor.

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